A Meta-Greedy Approach applied to a Multiobjective Scheduling Problem

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- 2 Example: a scheduling problem
- Some preliminary results





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- 3 Some preliminary results
- 4 Conclusion

## **Motivation**

### Mutliobjective problem

Need to handle antagonist objectives. Solutions can be incomparable (non-dominated).



### Techniques

Fast method for generating a set of non-dominated solutions (possibly Pareto-optimal).

Existing method: multiobjective metaheuristics, espilon-method,

Pareto set approximation (Papadimitriou, Yannakakis, 2000), ...

# **Beyond heuristics**

#### General methodology

Method for solving multiobjective problems: takes a problem as input and produces a heuristic.

Similar to multiobjective metaheuristic and greedy strategy. Restriction to the input problems: solutions can be constructed incrementally (as for greedy).

#### More precisely

Generalization of *greedy algorithms* when dealing with *multiple objectives*.

## Multiobjective

### Classical greedy

Any following incremental modification to a partial solution is chosen according to one criterion  $c_1$  (from red to green).



### Considering multiple objectives

A set of non-dominated solutions is constructed at each step.



# Main loop

### Algorithm

Each incremented solution (red) is considered at the next iteration:

for each iteration
for each solution in the population
 increment the solution in several ways
keep the best generated partial solutions



# Criteria specification

#### Required problem-specific specification

Similar to mutation and crossover operators for metaheuristic. Since each partial solutions need to be evaluated, criteria for comparing partial solutions need to be defined.

#### Remark

Intermediate criteria  $\neq$  final criteria. How to compare partial solutions in a *fair* way (good intermediate criteria)?



- 2 Example: a scheduling problem
  - 3 Some preliminary results

### 4 Conclusion

# Problem definition

### Workload and platform model

A parallel application consisting DAG, *i.e.* of a set of tasks with precedence constraints.

A set of completely linked heterogeneous processors subject to failures.



### Objectives

- obtain a feasible schedule (start and end times for each task)
- minimize the makespan (total duration) of the schedule
- minimize the failure probability of the schedule

# Existing mono-objective greedy heuristics

#### Yet another algorithm based on HEFT

An order is defined for assigning task to processor. Tasks are iteratively assigned to the processor that minimizes a single criterion (end time of the current task).



#### Example: a scheduling problem Meta-greedy implementation

### Intermediate criteria definition

Remark: each partial solution has the same assigned tasks. First criterion: makespan of the partial solution. Second criterion: reliability.

#### Issue

Does not degenerate into the HEFT heuristic.

Indeed, partial makespan  $\neq$  end time of the inserted task.

Idea: mix of both criteria: for equal makespans, solution with the lowest end time of the current task is better for time



- A meta-greedy approach
- 2 Example: a scheduling problem
- Some preliminary results

### 4 Conclusion

# Hypervolume indicator

#### Other multiobjective approaches

HEFT-sub HEFT with a subset of processors

HEFT-agg HEFT with aggregation

#### Experiments

31 instances were generated (from Strassen, Gaussian elimination, and Cholesky decomposition).

The hypervolume of the meta-greedy is better than HEFT-sub in 93% and always better than HEFT-agg.

## Specific case

The graph is generated from the Strassen algorithm on a random platform.



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### Some preliminary results Set coverage indicator

Proportion of solutions in the column that are dominated by the row.



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- A meta-greedy approach
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#### Conclusion

### Conclusion and future directions

#### Main contributions

- Propose a generic approach (on the same level as greedy and metaheuristic designs) that can be applied to many problems.
- Assess its efficiency on a scheduling problem.
- Raise principal issue: intermediate criteria selection (comparing partial solutions).

### Perspective

- Use other task orderings (HSA, BSA) and other scheduling policies.
- Complete study of other combinatorial problems (knapsack, ...).

#### Conclusion

### Set limitation size

### Preference ordering

If too much generated solutions: selection among non-dominated solutions (active field of research).

Indicator-based proposition by Zitzler and Thiele (2009): keep a subset of solutions such that the indicator is maximized.

Parameters of the produced heuristics: indicator and maximum size.



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