# Mapping filter services on heterogeneous platforms To appear in IPDPS 2009

#### Anne Benoit, Fanny Dufossé, Yves Robert

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Anne Benoit, Fanny Dufossé, Yves Robert () Mapping filter services on heterogeneous plati

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The problem:

- treatment of a data flow
- filter services with selectivity  $\sigma$  and cost c
- precedence constraints between services
- servers with speed s
- one-to-one mappings

The objective:

- minimize the period
- minimize the latency

For services of selectivity less than one

- grep
- web services
- Select-Project-Join query optimization

#### • ...

Related problems:

- component testing
- unsupervised systems



### Period

- General structure of optimal solutions
- Case of homogeneous servers
- NP-completeness of MINPERIOD-HET
- Integer linear program

## Latency

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# Bi-criteria problem

5 Heuristics

# 6 Experiments

# Conclusion

The problems depend on:

- the criteria: MINPERIOD, MINLATENCY or BICRITERIA
- $\bullet$  the platform:  ${\rm HOM}$  or  ${\rm HET}$
- $\bullet$  the dependence constraints:  $\mathrm{NoPREC}$  or  $\mathrm{PREC}$

The problems depend on:

- the criteria: MINPERIOD, MINLATENCY or BICRITERIA
- the platform: HOM or HET
- the dependence constraints: NOPREC or PREC

The instances:  $\mathcal{A} = (\mathcal{F}, \mathcal{G}, \mathcal{S})$  with:

- The services:  $\mathcal{F} = \{C_1, C_2, \dots, C_n\}$
- $\bullet$  The precedence constraints:  $\mathcal{G} \subset \mathcal{F} \times \mathcal{F}$

• The servers: 
$$\mathcal{S} = \{S_1, S_2, \dots, S_p\}$$

Example for 3 independent services: The plan?



The mapping?

 $(C_1, S_2), (C_2, S_1), (C_3, S_3)$  $(C_1, S_3), (C_2, S_2), (C_3, S_1)$ 



Figure: Chaining services.



Figure: Combining selectivities

$$\begin{aligned} \mathcal{P} &= \max\left(\frac{c_1}{s_1}, \frac{\sigma_1 c_2}{s_2}, \frac{\sigma_1 \sigma_2 c_3}{s_3}\right) \quad \mathcal{P} = \max\left(\frac{c_1}{s_1}, \frac{c_2}{s_2}, \frac{\sigma_1 \sigma_2 c_3}{s_3}\right) \\ \mathcal{L} &= \frac{c_1}{s_1} + \frac{\sigma_1 c_2}{s_2} + \frac{\sigma_1 \sigma_2 c_3}{s_3} \quad \mathcal{L} = \max\left(\frac{c_1}{s_1}, \frac{c_2}{s_2}\right) + \frac{\sigma_1 \sigma_2 c_3}{s_3} \end{aligned}$$

# Example

• 
$$c_1 = 1, c_2 = 4, c_3 = 10$$
  
•  $\sigma_1 = \frac{1}{2}, \sigma_2 = \sigma_3 = \frac{1}{3}$ 

• 
$$s_1 = 1$$
,  $s_2 = 2$  and  $s_3 = 3$ 

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# Example

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$$c_1 = 1$$
,  $c_2 = 4$ ,  $c_3 = 10$   
•  $\sigma_1 = \frac{1}{2}$ ,  $\sigma_2 = \sigma_3 = \frac{1}{3}$   
•  $s_1 = 1$ ,  $s_2 = 2$  and  $s_3 = 3$ 



Figure: Optimal plan for period.

Figure: Optimal plan for latency

$$L = \frac{13}{6}$$
$$P = \frac{4}{3}$$

P = 1 $L = \frac{5}{2}$ 

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# General structure of optimal solutions

## The instance : $C_1, ..., C_n, S_1, ..., S_n$ with

- $\sigma_1, ..., \sigma_p \le 1$
- $\sigma_{p+1}, ..., \sigma_n \geq 1$

# General structure of optimal solutions

The instance :  $C_1, ..., C_n, S_1, ..., S_n$  with

- $\sigma_1, ..., \sigma_p \le 1$
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Figure: General structure

- The instance :  $C_1, ..., C_n$  with
  - $c_1 \leq c_2 \leq \ldots \leq c_p$
  - $\sigma_1, ..., \sigma_p < 1$
  - $\sigma_{p+1}, ..., \sigma_n \ge 1$

The matching:  $C_1 \rightarrow C_2 \rightarrow ... \rightarrow C_p$ 

Computing the optimal subgraph for *C* in the graph *G*: Let  $D = \max_i \{ \log \sigma_i \}$ . We construct a network flow graph *W* with:

- a source s
- a node  $f_i$  by service in G
- a sink node t
- an edge  $s > f_i$  with capacity  $+\infty$  if  $C_i$  is ancestor of C in G, D else
- an edge  $f_i f_j$  of capacity  $+\infty$  if  $C_j$  is an ancestor of  $C_i$  in G
- an edge  $f_i > t$  with capacity  $D + \log \sigma_i$

The set of services on the side of s in a min-cut is the optimal subset of predecessors for latency.

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The set of services on the side of s in a min-cut is the optimal subset of predecessors for latency.

Optimal algorithm: at each step place the available service with minimal possible period.



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## Problem (RN3DM)

Given an integer vector A = (A[1], ..., A[n]) of size n, does there exist two permutations  $\lambda_1$  and  $\lambda_2$  of  $\{1, 2, ..., n\}$  such that

 $\forall 1 \leq i \leq n, \quad \lambda_1(i) + \lambda_2(i) = A[i]$ 

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The associated instance :

• 
$$c_i = 2^{A[i]}$$

• 
$$\sigma_i = 1/2$$

• 
$$s_i = 2^i$$

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$$c_{i} = 2^{A[i]}$$

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$$P = 2$$

$$\forall 1 \le i \le n, \quad \lambda_{1}(i) + \lambda_{2}(i) \ge A[i]$$

$$\iff \forall 1 \le i \le n, \quad \left(\frac{1}{2}\right)^{\lambda_{1}(i)-1} \times \frac{2^{A[i]}}{2^{\lambda_{2}(i)}} \le 1$$

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#### Proposition

For any K > 0, there exists no K-approximation algorithm for MINPERIOD-NOPREC-HET, unless P=NP.

### Proposition

For any K > 0, there exists no K-approximation algorithm for MINPERIOD-NOPREC-HET, unless P=NP.

Reduction from RN3DM:

• 
$$c_i = K^{A[i]-1}$$

• 
$$\sigma_i = 1/K$$

• 
$$s_i = K^i$$

- $t_{i,u} = 1$  if service  $C_i$  is assigned to server  $S_u$
- $s_{i,j} = 1$  if service  $C_i$  is an ancestor of  $C_j$
- *M* is the logarithm of the optimal period

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- *M* is the logarithm of the optimal period

The constraints:

•  $\forall i, \quad \sum_{u} t_{i,u} = 1$ •  $\forall u, \quad \sum_{i} t_{i,u} = 1$ •  $\forall i, j, k, \quad s_{i,j} + s_{j,k} - 1 \le s_{i,k}$ •  $\forall i, s_{i,i} = 0$ •  $\forall i, \quad \log c_i - \sum_{u} t_{i,u} \log s_u + \sum_{k} s_{k,i} \log \sigma_k \le M$ 

The objective function: Minimize M

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# Structure of the optimal plan

### Proposition

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Let  $C_1, ..., C_n, S_1, ..., S_n$  be an instance of MINLATENCY. Then, the optimal latency is obtained with a plan G such that, for any  $v_1 = (C_{i_1}, S_{u_1})$ ,  $v_2 = (C_{i_2}, S_{u_2})$ ,

- If d<sub>i1</sub>(G) = d<sub>i2</sub>(G), they have the same predecessors and the same successors in G.
- 2 If  $d_{i_1}(G) > d_{i_2}(G)$  and  $\sigma_{i_2} \le 1$ , then  $c_{i_1}/s_{u_1} < c_{i_2}/s_{u_2}$ .
- 3 All nodes with a service of selectivity  $\sigma_i > 1$  are leaves  $(d_i(G) = 0)$ .





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```
Data: n services of cost c_1 \leq \cdots \leq c_n and of selectivities \sigma_1, \dots, \sigma_n \leq 1
Result: a plan G optimizing the latency
G is the graph reduced to node C_1;
for i = 2 to n do
    for i = 0 to i - 1 do
        Compute the completion time t_i of C_i in G with predecessors
        C_1, ..., C_i
    end
    Choose j such that t_i = \min_k \{t_k\};
    Add the node C_i and the edges C_1 \rightarrow C_i, \ldots, C_i \rightarrow C_i to G;
end
```

**Algorithm 1**: Optimal algorithm for MINLATENCY-NOPREC-HOM.

G is the graph reduced to the node C of minimal cost with no predecessor in  $\mathcal{G};$ 

```
for i = 2 to n do
    Let S be the set of services not yet in G and such that their set of
    predecessors in \mathcal{G} is included in G;
   for C \in S do
       for C' \in G do
           Compute the set S' minimizing the product of selectivities
           among services of latency less than L_G(C'), and including all
           predecessors of C in \mathcal{G}:
       end
       Let S_C be the set that minimizes the latency of C in G and L_C be
       this latency;
   end
```

```
Choose a service C such that L_C = \min\{L_{C'}, C' \in S\};
Add to G the node C, and \forall C' \in S_C, the edge C' \to C;
```

#### end

Algorithm 2: Optimal algorithm for MINLATENCY-PREC-HOM.

# Example

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# Example





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#### Lemma

Let  $C_1, ..., C_n, S_1, ..., S_n$  be an instance such that  $\forall i, c_i$  and  $s_i$  are integer power of 2 and  $\sigma_i \leq \frac{1}{2}$ . Then the optimal latency is obtained with a plan G such that

- **1** Proposition 2 is verified;
- **2** for all nodes  $(C_{i_1}, S_{u_1})$  and  $(C_{i_2}, S_{u_2})$  with  $d_{i_1}(G) = d_{i_2}(G)$ , we have  $\frac{c_{i_1}}{s_{u_1}} = \frac{c_{i_2}}{s_{u_2}}$ .

#### Lemma

Let  $C_1, ..., C_n, S_1, ..., S_n$  be an instance such that  $\forall i, c_i$  and  $s_i$  are integer power of 2 and  $\sigma_i \leq \frac{1}{2}$ . Then the optimal latency is obtained with a plan G such that

- Proposition 2 is verified;
- **2** for all nodes  $(C_{i_1}, S_{u_1})$  and  $(C_{i_2}, S_{u_2})$  with  $d_{i_1}(G) = d_{i_2}(G)$ , we have  $\frac{c_{i_1}}{s_{u_1}} = \frac{c_{i_2}}{s_{u_2}}$ .
- $c_i = 2^{A[i] \times n + (i-1)}$ •  $\sigma_i = (\frac{1}{2})^n$ •  $s_i = 2^{n \times (i+1)}$ •  $l = 2^n - 1$

#### Proposition

For any K > 0, there exists no K-approximation algorithm for MINLATENCY-NOPREC-HET, unless P=NP.

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For any K > 0, there exists no K-approximation algorithm for MINLATENCY-NOPREC-HET, unless P=NP.

#### Reduction from $\operatorname{RN3DM}$

•  $c_i = K^{A[i] \times n + (i-1)}$ •  $\sigma_i = \left(\frac{1}{K}\right)^n$ •  $s_i = K^{n \times (i+1)}$ •  $L = \frac{K^n - 1}{K - 1}$ 



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## Conclusion

- z(i, u, e) = 1 if the service C<sub>i</sub> is associated to the server S<sub>u</sub> and its set of predecessors is e ⊂ C.
- t(i) is the completion time of  $C_i$
- *M* is the optimal latency

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- *M* is the optimal latency

The constraints:

• 
$$\forall u \in S$$
,  $\sum_{i \in C} \sum_{e \subset C} z(i, u, e) = 1$   
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•  $\forall i \in C$ ,  $\sum_{u \in S} \sum_{e \subset C} z(i, u, e) = 1$   
•  $\forall i, i' \in C, \forall u, u' \in S, \forall e, e' \subset C, e \nsubseteq e', i \in e', z(i, u, e) + z(i', u', e') \le 1$ 

• 
$$\forall u \in S, \forall e \subset C, \forall i \in e, \ z(i, u, e) = 0$$

- z(i, u, e) = 1 if the service C<sub>i</sub> is associated to the server S<sub>u</sub> and its set of predecessors is e ⊂ C.
- t(i) is the completion time of  $C_i$
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,  $\sum_{i \in C} \sum_{e \in C} z(i, u, e) = 1$   
•  $\forall i \in C$ ,  $\sum_{u \in S} \sum_{e \in C} z(i, u, e) = 1$   
•  $\forall i, i' \in C, \forall u, u' \in S, \forall e, e' \in C, e \notin e', i \in e', z(i, u, e) + z(i', u', e') \leq 1$   
•  $\forall u \in S, \forall e \in C, \forall i \in e, z(i, u, e) = 0$   
•  $\forall i \in C, \forall e \in C, \forall k \in e, t(i) \geq \sum_{u \in S} z(i, u, e) \left(\frac{c_i}{s_u} * \prod_{C_j \in e} \sigma_j + t(k)\right)$   
•  $\forall i \in C, t(i) \geq \sum_u z(i, u, e) \frac{c_i}{s_u} * \prod_{C_j \in e} \sigma_j$   
•  $\forall i \in C, t(i) \leq M$ 

The objective function: Minimize M

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**Data**: *n* services of cost  $c_1 \leq \cdots \leq c_n$  and of selectivities  $\sigma_1, ..., \sigma_n \leq 1$ and a maximum throughput K

**Result**: a plan *G* optimizing the latency with a throughput less than K *G* is the graph reduced to node  $C_1$ ;

for i = 2 to n do

for j = 0 to i - 1 do Compute the completion time  $t_j$  of  $C_i$  in G with predecessors  $C_1, ..., C_j$ ; end Let  $S = \{k | c_i \prod_{0 \le k < i} \sigma_k \le K\}$ ; Choose j such that  $t_j = \min_{k \in S} \{t_k\}$ ; Add the node  $c_i$  and the edges  $C_1 \rightarrow C_i, ..., C_i \rightarrow C_i$  to G;

#### end

Algorithm 3: Optimal algorithm for latency with a fixed throughput.

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Integer linear program

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sigma-inc We place services on a chain in increasing order of  $\sigma$ .

short service/fast server We associate the service with shortest cost to the server with fastest speed.

long service/fast server We associate the service with largest cost with the server with fastest speed.

opt-homo We randomly associate services to servers.

- greedy min This simple heuristic consists in running successively the four previous heuristics on the problem instance, and returning as a result the best of the four solutions.
  - random This last heuristic is fully random: we randomly associate services and servers, and we randomly place these pairs on a linear chain.

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## Conclusion

The instances:

- independent services
- the cost of services:  $1 \le c \le 100$
- the selectivities: 0,01  $\leq \sigma \leq 1$
- the speed of servers:  $1 \le s \le 100$



Figure: Experiment 1: general experiment.

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Image: A match a ma



Figure: Experiment 1: general experiment.



Figure: Experiment 2: with small selectivity.

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Figure: Experiment 3: with high selectivity.

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Figure: Experiment 4: with low speed.

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Figure: Experiment 5: with low heterogeneity.

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Figure: Experiment 1: Computing times.

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The results:

- MINLATENCY-HOM is polynomial
- MINPERIOD-HET is NP-complete
- MINLATENCY-HET is NP-complete
- BICRITERIA-HOM is polynomial
- The experiments on MINPERIOD-NOPREC-HET:
  - heuristics close to the optimal for small instances
  - better performance than random

Future work:

model with communication costs

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