Strategies for Replica Placement in Tree Networks

http://graal.ens-lyon.fr/~lmarchal/scheduling/

2 avril 2009

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- Replica placement in tree networks
- Set of clients (tree leaves): flows of requests with QoS constraints, known in advance

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How many replicas required? Which locations? Total replica cost?

▶ Handle all client requests, and minimize cost of replicas

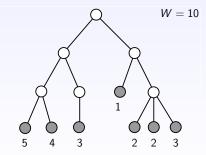
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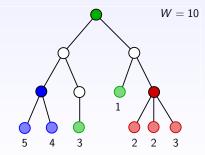
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- Several policies to assign replicas



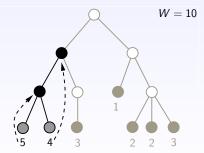
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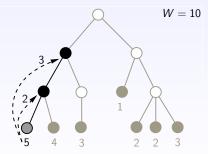
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Outline





- 3 Complexity results
- 4 Linear programming formulation
- 5 Heuristics for the REPLICA COST problem

6 Conclusion

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- **Tree edge:** $l \in \mathcal{L}$ (communication link between nodes)
 - Communication time comm₁
 - Bandwidth limit BW₁

Tree notations

- r: tree root
- children(j): set of children of node $j \in \mathcal{N}$
- ▶ parent(k): parent in the tree of node $k \in \mathcal{N} \cup \mathcal{C}$
- link *l* : *k* → parent(*k*) = *k'*. Then succ(*l*) is the link *k'* → parent(*k'*) (when it exists)
- Ancestors(k): set of ancestors of node k
- If k' ∈ Ancestors(k), then path[k → k']: set of links in the path from k to k'

subtree(k): subtree rooted in k, including k.

- Goal: place replicas to process client requests
- ► Client i ∈ C: Servers(i) ⊆ N set of servers responsible for processing its requests
- ► $r_{i,s}$: number of requests from client *i* processed by server *s* ($\sum_{s \in \text{Servers}(i)} r_{i,s} = r_i$)

▶ $R = \{s \in \mathcal{N} | \exists i \in C, s \in \text{Servers}(i)\}$: set of replicas

Constraints

Server capacity

$$\forall s \in R, \sum_{i \in \mathcal{C} | s \in \text{Servers}(i)} r_{i,s} \leq W_s$$

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QoS

$$\forall i \in \mathcal{C}, \forall s \in \text{Servers}(i), \sum_{l \in path[i \rightarrow s]} \text{comm}_l \leq q_i.$$

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Objective function





Objective function

- Min $\sum_{s \in R} \operatorname{sc}_s$
- Restrict to case where sc_s = W_s
- REPLICA COST problem: no QoS nor bandwidth constraints; heterogeneous servers

 REPLICA COUNTING problem: idem, but homogeneous platforms

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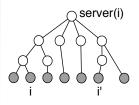
Single server – Each client *i* is assigned a single server server(*i*), that is responsible for processing all its requests. Multiple servers – A client *i* may be assigned several servers in a set Servers(*i*). Each server $s \in$ Servers(*i*) will handle a fraction $r_{i,s}$ of the requests.

In the literature: single server policy with additional constraint.

Closest policy

Closest: single server policy

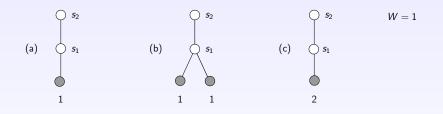
- Server of client *i* is constrained to be first server found on the path that goes from *i* upwards to the tree root
- Consider a client *i* and its server server(*i*): ∀*i*' ∈ subtree(server(*i*)), server(*i*') ∈ subtree(server(*i*))
- Requests from i' cannot "traverse" server(i) and be served higher



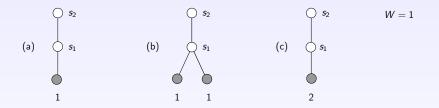
Upwards and Multiple policy

- New policies not studied in the literature
- Upwards: Closest constraint is relaxed
- Multiple: relax single server restriction
- Expect more solutions with new policies, at a lower cost

QoS constraints may lower difference between policies

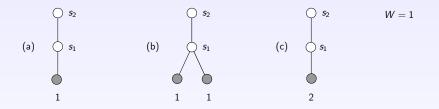


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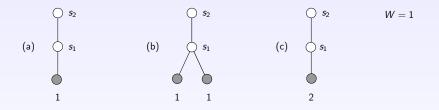
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▶ (a): solution for all policies



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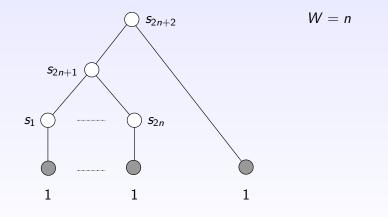
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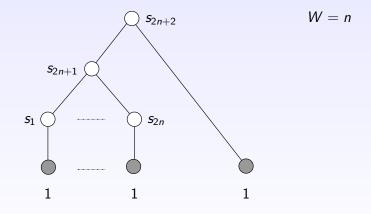
- (a): solution for all policies
- (b): no solution with Closest
- ► (c): no solution with *Closest* nor *Upwards*

Upwards versus Closest



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Upwards versus Closest

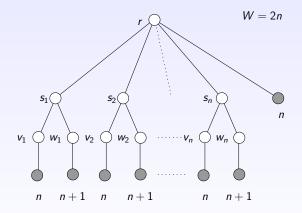


• Upwards: 3 replicas in s_{2n} , s_{2n+1} and s_{2n+2}

• Closest: at least n + 2 replicas (replica in s_{2n+1} or not)

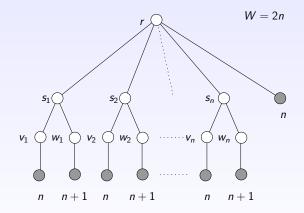
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Multiple versus Upwards



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Multiple versus Upwards

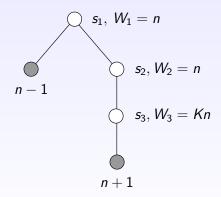


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- Multiple: n+1 replicas / Upwards: 2n replicas
- Multiple twice better than Upwards.
- ▶ Performance ratio: open problem.

Multiple versus Upwards

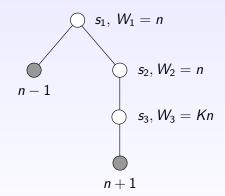
► Replica Cost



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Multiple versus Upwards

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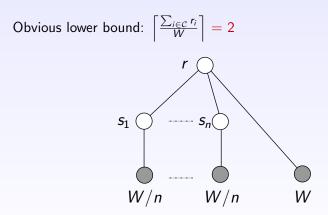


- Multiple: cost 2n / Upwards: cost (K+1)n
- Multiple arbitrarily better than Upwards

Lower bound for the $\operatorname{Replica}$ Counting problem

Obvious lower bound: \sum

$$\frac{\sum_{i\in\mathcal{C}}r_i}{W}$$



All policies require n + 1 replica (one at each node).

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	Replica Counting	Replica Cost
	Homogeneous	Heterogeneous
Closest	polynomial [Cidon02,Liu06]	
Upwards		
Multiple		

 Closest/Homogeneous: only known result (Cidon et al. 2002, Liu et al. 2006)

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- Closest/Homogeneous: only known result (Cidon et al. 2002, Liu et al. 2006)
- Multiple/Homogeneous: nice algorithm to prove polynomial complexity
- Upwards/Homogeneous: surprisingly, NP-complete
- ► All instances for the Heterogeneous case are NP-complete

3-pass algorithm:

- Select nodes which can handle W requests
- Select some extra servers to fulfill remaining requests

Decide which requests are processed where

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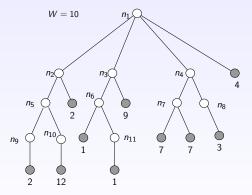
Example to illustrate algorithm (informally)

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Example to illustrate algorithm (informally)

Proof of optimality: any optimal solution can be transformed into a solution similar to the one of the algorithm (moving requests from one server to another)

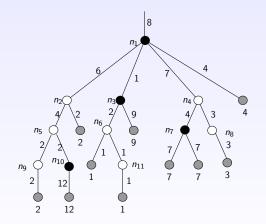


Initial network

The example network

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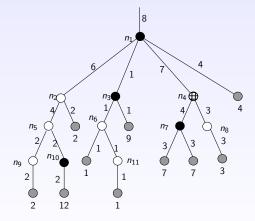
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Placing *saturated* replicas

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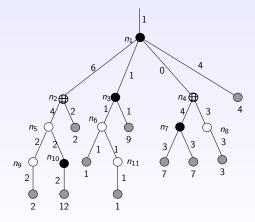




Placing extra replicas: n_4 has maximum useful flow

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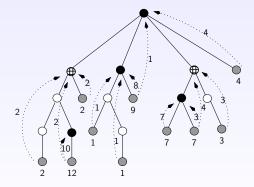




Placing extra replicas: n_2 is of maximum useful flow 1

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Deciding where requests are processed

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Upwards/Homogeneous

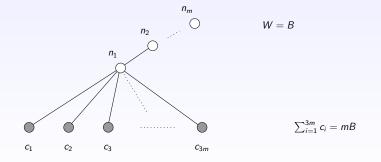
The REPLICA COUNTING problem with the Upwards strategy is NP-complete in the strong sense

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Reduction from 3-PARTITION

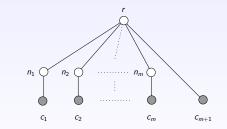


Heterogeneous network: REPLICA COST problem

► All three instances of the REPLICA COST problem with heterogeneous nodes are NP-complete

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- Reduction from 2-PARTITION

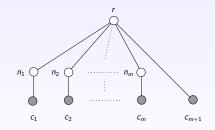


 $\sum_{i=1}^{m} c_i = S$, $c_{m+1} = 1$, $W_j = c_j$, $W_r = S/2 + 1$

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Heterogeneous network: REPLICA COST problem

- All three instances of the REPLICA COST problem with heterogeneous nodes are NP-complete
- Reduction from 2-PARTITION



 $\sum_{i=1}^{m} c_i = S, c_{m+1} = 1, W_j = c_j, W_r = S/2 + 1$ Solution with total storage cost S + 1?

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Linear programming

General instance of the problem

- Heterogeneous tree
- QoS and bandwidth constraints
- Closest, Upwards and Multiple policies
- Integer linear program: no efficient algorithm
- Absolute lower bound if program solved over the rationals (using the GLPK software)

Closest/Upwards LP formulation

Linear program: variables

x_j: boolean variable equal to 1 if j is a server (for one or several clients)

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• $y_{i,j}$: boolean variable equal to 1 if j = server(i)

• If
$$j \notin Ancests(i)$$
, $y_{i,j} = 0$

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 - If $j \notin Ancests(i)$, $y_{i,j} = 0$
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 - If $j \notin Ancests(i)$, $y_{i,j} = 0$
- *z_{i,l}*: boolean variable equal to 1 if link *l* ∈ path[*i* → *r*] used when *i* accesses server(*i*)

• If $l \notin path[i \rightarrow r]$, $z_{i,l} = 0$

Objective function: $\sum_{j \in \mathcal{N}} \operatorname{sc}_j x_j$

► Servers:
$$\forall i \in C, \sum_{j \in \text{Ancestors}(i)} y_{i,j} = 1$$

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- Links: $\forall i \in C, z_{i,i \rightarrow \text{parent}(i)} = 1$
- ▶ Conservation: $\forall i \in C, \forall I : j \rightarrow j' = parent(j) \in path[i \rightarrow r],$

 $z_{i,\mathrm{succ}(I)} = z_{i,I} - y_{i,j'}$

- ► Servers: $\forall i \in C, \sum_{j \in Ancestors(i)} y_{i,j} = 1$
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- Server capacity: $\forall j \in \mathcal{N}, \sum_{i \in \mathcal{C}} r_i y_{i,j} \leq W_j x_j$
- ▶ Bandwidth limit: $\forall I \in \mathcal{L}, \sum_{i \in \mathcal{C}} r_i z_{i,l} \leq BW_I$

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- ▶ Bandwidth limit: $\forall I \in \mathcal{L}, \sum_{i \in \mathcal{C}} r_i z_{i,i} \leq \mathsf{BW}_I$
- ▶ QoS constraint: $\forall i \in C, \forall j \in Ancestors(i), dist(i, j)y_{i,j} \leq q_i$

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- Links: $\forall i \in \mathcal{C}, z_{i,i \rightarrow \text{parent}(i)} = 1$
- ► Conservation: $\forall i \in C, \forall l : j \to j' = \text{parent}(j) \in \text{path}[i \to r],$ $z_{i,\text{succ}(l)} = z_{i,l} - y_{i,j'}$

• Server capacity: $\forall j \in \mathcal{N}, \sum_{i \in \mathcal{C}} r_i y_{i,j} \leq W_i x_i$

- ▶ Bandwidth limit: $\forall I \in \mathcal{L}, \sum_{i \in \mathcal{C}} r_i z_{i,i} \leq \mathsf{BW}_I$
- ▶ QoS constraint: $\forall i \in C, \forall j \in Ancestors(i), dist(i, j)y_{i,j} \leq q_i$

► Closest constraint: $\forall i \in C, \forall j \in \text{Ancestors}(i) \setminus \{r\}, \forall i' \in C \cap \text{subtree}(j), y_{i,j} + z_{i',j \rightarrow \text{parent}(j)} \leq 1$

Multiple formulation

Multiple

- Similar formulation, with
 - y_{i,j}: integer variable = nb requests from client i processed by node j

- $z_{i,l}$: integer variable = nb requests flowing through link l
- Constraints are slightly modified

An ILP-based lower bound

- Solving over the rationals: solution for all practical values of the problem size
 - Not very precise bound
 - Upwards/Closest equivalent to Multiple when solved over the rationals

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An ILP-based lower bound

- Solving over the rationals: solution for all practical values of the problem size
 - Not very precise bound
 - Upwards/Closest equivalent to Multiple when solved over the rationals
- Integer solving: limitation to $s \leq 50$ nodes and clients
- Mixed bound obtained by solving the *Multiple* formulation over the rational and imposing only the x_i being integers
 - Resolution for problem sizes $s \le 400$
 - Improved bound: if a server is used only at 50% of its capacity, the cost of placing a replica at this node is not halved as it would be with x_j = 0.5.

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- Heuristics
- Experiments



Heuristics

\blacktriangleright Polynomial heuristics for the $\operatorname{RepLICA}$ Cost problem

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- Heterogeneous platforms
- No QoS nor bandwidth constraints

Heuristics

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- Experimental assessment of the relative performance of the three policies

Heuristics

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- No QoS nor bandwidth constraints
- Experimental assessment of the relative performance of the three policies

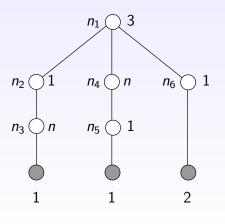
- Traversals of the tree, bottom-up or top-down
- ► Worst case complexity O(s²), where s = |C| + |N| is problem size

Closest Top Down All CTDA

- Breadth-first traversal of the tree
- When a node can process the requests of all the clients in its subtree, node chosen as a server and exploration of the subtree stopped
- Procedure called until no more servers are added

Closest Top Down All CTDA

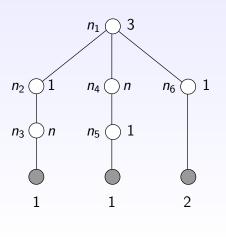
- Breadth-first traversal of the tree
- When a node can process the requests of all the clients in its subtree, node chosen as a server and exploration of the subtree stopped
- Procedure called until no more servers are added
- Choosing n_2 , n_4 and then n_1



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Closest Top Down Largest First CTDLF

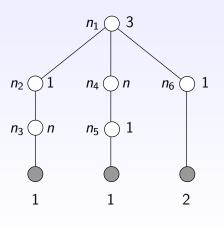
- Traversal of the tree, treating subtrees that contains most requests first
- When a node can process the requests of all the clients in its subtree, node chosen as a server and traversal stopped
- Procedure called until no more servers are added
- Choosing n₂ and then n₁



Closest Bottom Up CBU

- Bottom-up traversal of the tree
- When a node can process the requests of all the clients in its subtree, node chosen as a server

Choosing n₃, n₅, n₁



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Heuristics for Upwards

Upwards Top Down **UTD**

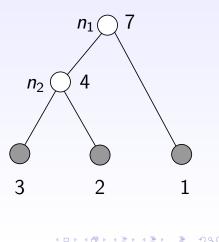
2-pass algorithm

 Select first saturating nodes, then extra nodes

Heuristics for Upwards

Upwards Top Down **UTD**

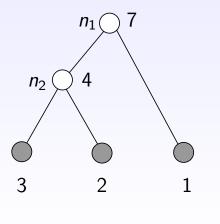
- 2-pass algorithm
- Select first saturating nodes, then extra nodes
- ► Choosing n₂ (for c₁) and in second pass n₁ (for c₂, c₃)



Heuristics for Upwards

Upwards Big Client First UBCF

- Sorting clients by decreasing request numbers, and finding the server of minimal available capacity to process its requests.
- Choosing n₂ for c₁, n₁ for c₂ and n₁ for c₃

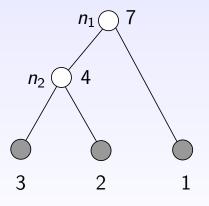


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Heuristics for *Multiple*

A greedy heuristic **MG**, similar to Pass 3 of the polynomial algorithm for *Multiple*/Homogeneous: fill all servers as much as possible in a bottom-up fashion

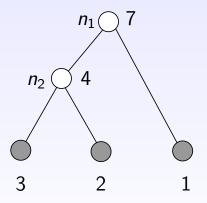


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Heuristics for Multiple

A greedy heuristic **MG**, similar to Pass 3 of the polynomial algorithm for *Multiple*/Homogeneous: fill all servers as much as possible in a bottom-up fashion



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- MG affects 4 requests to n₂, and then the remaining 2 requests to n₁
- CTDLF better on this example: selects n₁ only

Heuristics for Multiple

- A top-down and a bottom-up heuristic in 2-passes (MTD, MBU)
- Heuristic MixedBest MB which picks up best result over all heuristics: solution for the *Multiple* policy

Plan of experiments

- Assess impact of the different access policies
- Assess performance of the polynomial heuristics

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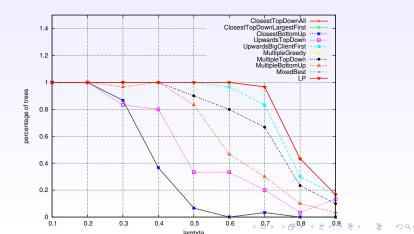
Plan of experiments

- Assess impact of the different access policies
- Assess performance of the polynomial heuristics
- Important parameter:

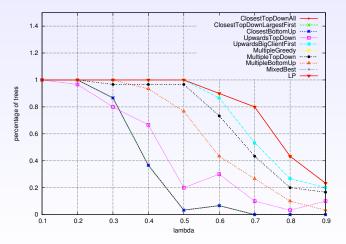
$$\lambda = \frac{\sum_{i \in \mathcal{C}} r_i}{\sum_{j \in \mathcal{N}} W_i}$$

- ▶ 30 trees for each $\lambda = 0.1, 0.2, ..., 0.9$
- ▶ Problem size s = |C| + |N| such that $15 \le s \le 400$
- Computation of the LP lower bound for each tree

- Number of solutions for each lambda and each heuristic
- \blacktriangleright No LP solution \rightarrow No solution for any heuristic
- Homogeneous case

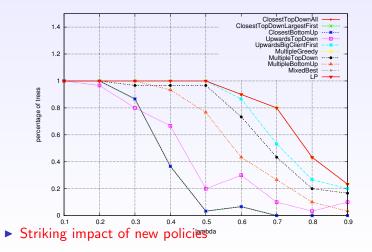


Heterogeneous trees: similar results



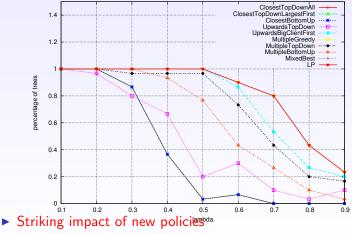
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Heterogeneous trees: similar results



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Heterogeneous trees: similar results



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MG and MB always find the solution

 Distance of the result (in terms of replica cost) of the heuristic to the lower bound

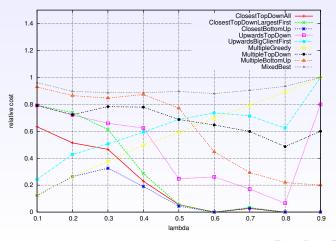
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- Distance of the result (in terms of replica cost) of the heuristic to the lower bound
- *T_λ*: subset of trees with a solution
- Relative cost:

$$rcost = rac{1}{|T_{\lambda}|} \sum_{t \in T_{\lambda}} rac{cost_{LP}(t)}{cost_h(t)}$$

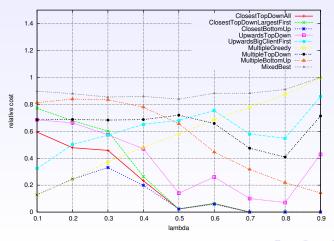
- cost_{LP(t)}: lower bound cost on tree t
- ► cost_h(t): heuristic cost on tree t; cost_h(t) = +∞ if h did not find any solution

Homogeneous results



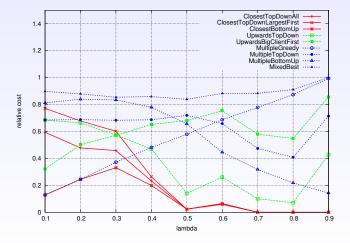
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Heterogeneous results - similar to the homogeneous case



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Results - Hierarchy



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Summary

- Striking effect of new policies: many more solutions to the REPLICA PLACEMENT problem

Best Multiple heuristic (MB) always at 85% of the lower bound: satisfactory result

Outline

Framework

- 2 Access policies
- 3 Complexity results
- 4 Linear programming formulation
- 5 Heuristics for the REPLICA COST problem

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6 Conclusion



Several papers on replica placement, but...

Related work

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…all consider only the *Closest* policy

Related work

- Several papers on replica placement, but...
- …all consider only the Closest policy
- ▶ REPLICA PLACEMENT in a general graph is NP-complete
- Wolfson and Milo: impact of the write cost, use of a minimum spanning tree for updates. Tree networks: polynomial solution
- Cidon et al (multiple objects) and Liu et al (QoS constraints): polynomial algorithms for homogeneous networks.
- Kalpakis et al: NP-completeness of a variant with bidirectional links (requests served by any node in the tree)
- Karlsson et al: comparison of different objective functions and several heuristics. No QoS, but several other constraints.
- Tang et al: real QoS constraints
- ► Rodolakis et al: *Multiple* policy but in a very different context

Conclusion

- Introduction of two new policies for the REPLICA PLACEMENT problem
- ► Upwards and Multiple: natural variants of the standard Closest approach → surprising they have not already been considered

Conclusion

- Introduction of two new policies for the REPLICA PLACEMENT problem
- ► Upwards and Multiple: natural variants of the standard Closest approach → surprising they have not already been considered
- Theoretical side Complexity of each policy, for homogeneous and heterogeneous platforms
- Practical side
- Design of several heuristics for each policy
 - Comparison of their performance
 - Striking impact of the policy on the result
 - Use of a LP-based lower bound to assess the absolute performance, which turns out to be quite good.