

CR-08: Scheduling (Ordonnancement)

Loris Marchal, CR CNRS

Scheduling:

- ▶ part of Optimization Research
- ▶ allocate **resources** to **tasks** to optimize some **performance metric**

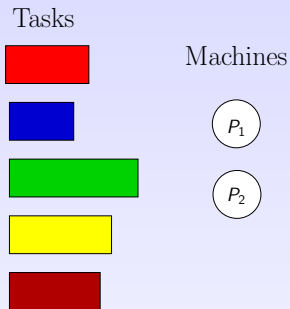
Context:

- ▶ computer systems
- ▶ distributed computing platforms

Pre-requisite (recommended):

- ▶ Parallel Algorithms (CB-04)

Example 1:

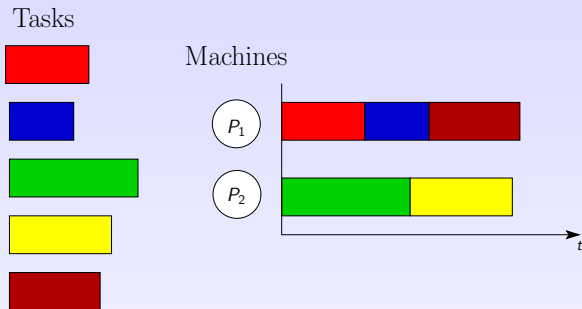


Objectives:

- ▶ Minimizing total execution time (C_{max})
- ▶ Minimizing average execution time $\sum_i C_i$
- ▶ Minimizing weighted sum of execution time $\sum_i w_i C_i$
- ▶ With deadlines, minimize the number of late jobs

Results: NP-completeness, algorithms, approximation algorithms, (in-)approximation bounds

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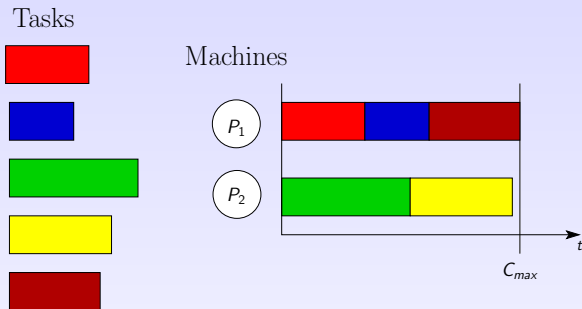


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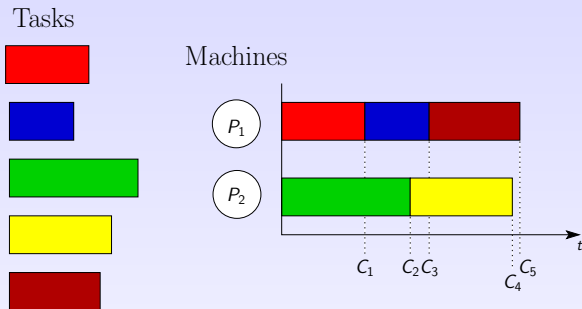


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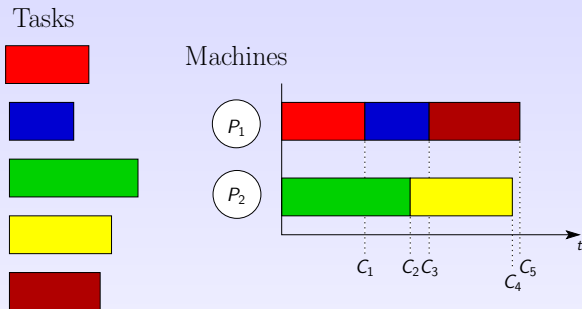


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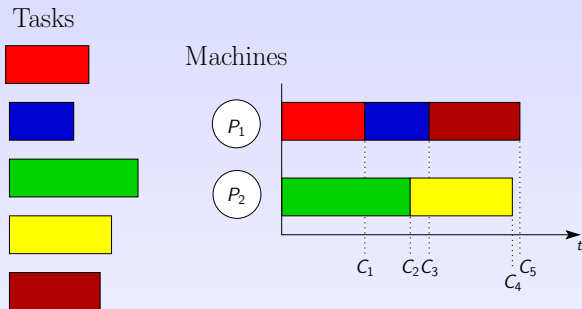


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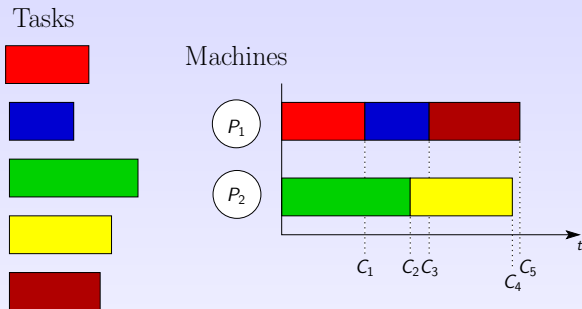


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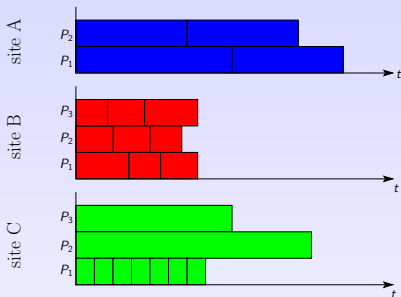


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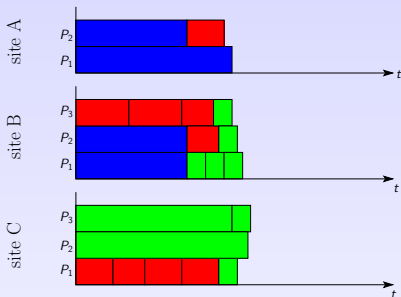
Context:

- ▶ Multiple organization have their own cluster
- ▶ Sharing resources to increase performance
- ▶ Selfishness: organization will not participate if the performance for its tasks is decreased

Results:

- ▶ Bounds on ratio with/without selfishness
- ▶ Approximation algorithms
- ▶ Use of game theory to model users...

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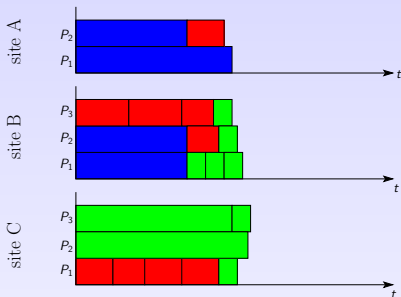
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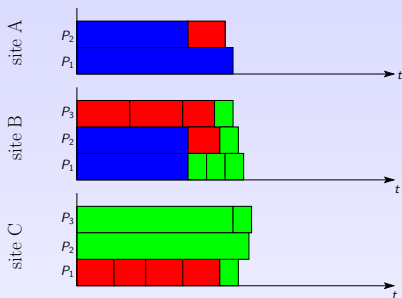
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General outline:

1. Classical scheduling methods and results (~ 3 courses)
 - ▶ Classical problems (List scheduling, etc.)
 - ▶ Application modeling and corresponding results
 - ▶ NP-completeness, approximation algorithms
 - ▶ Online and non-clairvoyant scheduling
2. Better models for computing platforms (~ 4 courses)
 - ▶ Introducing communication costs
 - ▶ Divisible Load Scheduling, Steady-State
 - ▶ Communication/Computation Interference
3. New objectives and trends in scheduling (~ 6 courses)
 - ▶ Fault tolerance, robustness, energy consumption
 - ▶ Multi-organization scheduling
 - ▶ Game theory and scheduling
 - ▶ Stochastic methods
 - ▶ Multi-criteria optimization

Organization

- ▶ French or English (on demand)
- ▶ A few courses to practice article analysis

Exams:

- ▶ Bibliographic study, on (provided) articles (~ 2 per student)

mail: Loris.Marchal@ens-lyon.fr or room 335, 3rd floor

More info: graal.ens-lyon.fr/~lmarchal/scheduling/